

# 7.2

## Use the Converse of the Pythagorean Theorem

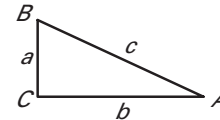
- Goal** • Use the Converse of the Pythagorean Theorem to determine if a triangle is a right triangle.

### Your Notes

#### THEOREM 7.2: CONVERSE OF THE PYTHAGOREAN THEOREM

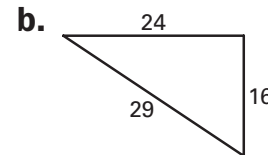
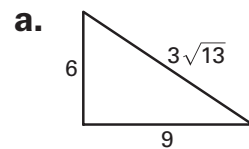
If the square of the length of the longest side of a triangle is equal to the sum of the squares of the lengths of the other two sides, then the triangle is a right triangle.

If  $c^2 = a^2 + b^2$ , then  $\triangle ABC$  is a right triangle.



#### Example 1 Verify right triangles

Tell whether the given triangle is a right triangle.



#### Solution

Let  $c$  represent the length of the longest side of the triangle. Check to see whether the side lengths satisfy the equation  $c^2 = a^2 + b^2$ .

$$\begin{aligned} \text{a. } (3\sqrt{13})^2 &\stackrel{?}{=} 6^2 + 9^2 \\ 9 \cdot 13 &\stackrel{?}{=} 36 + 81 \\ 117 &= 117 \quad \checkmark \end{aligned}$$

The triangle is a right triangle.

$$\begin{aligned} \text{b. } 29^2 &\stackrel{?}{=} 24^2 + 16^2 \\ 841 &\stackrel{?}{=} 576 + 256 \\ 841 &\neq 832 \end{aligned}$$

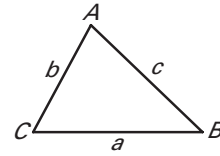
The triangle is not a right triangle.

## Your Notes

### THEOREM 7.3

If the square of the length of the longest side of a triangle is less than the sum of the squares of the lengths of the other two sides, then the triangle  $ABC$  is an acute triangle.

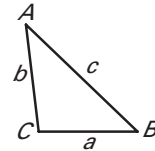
If  $c^2 < a^2 + b^2$ , then the triangle  $ABC$  is acute.



### THEOREM 7.4

If the square of the length of the longest side of a triangle is greater than the sum of the squares of the lengths of the other two sides, then the triangle  $ABC$  is an obtuse triangle.

If  $c^2 > a^2 + b^2$ , then the triangle  $ABC$  is obtuse.



### Example 2 Classify triangles

Can segments with lengths of 2.8 feet, 3.2 feet, and 4.2 feet form a triangle? If so, would the triangle be *acute*, *right*, or *obtuse*?

#### Solution

**Step 1** Use the Triangle Inequality Theorem to check that the segments can make a triangle.

$$\begin{array}{l|l|l} 2.8 + 3.2 = \underline{6} & 2.8 + 4.2 = \underline{7} & 3.2 + 4.2 = \underline{7.4} \\ \underline{6} > 4.2 & \underline{7} > 3.2 & \underline{7.4} > 2.8 \end{array}$$

**Step 2** Classify the triangle by comparing the square of the length of the longest side with the sum of squares of the lengths of the shorter sides.

$$c^2 \text{ ? } a^2 + b^2$$

Compare  $c^2$  with  $a^2 + b^2$ .

$$\underline{4.2}^2 \text{ ? } \underline{2.8}^2 + \underline{3.2}^2$$

Substitute.

$$\underline{17.64} \text{ ? } \underline{7.84} + \underline{10.24}$$

Simplify.

$$\underline{17.64} < \underline{18.08}$$

$c^2$  is less than  $a^2 + b^2$ .

The side lengths 2.8 feet, 3.2 feet, and 4.2 feet form an acute triangle.

The Triangle Inequality Theorem states that the sum of the lengths of any two sides of a triangle is greater than the length of the third side.

**Example 3** Use the Converse of the Pythagorean Theorem

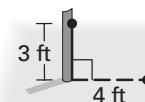
**Lights** You are helping install a light pole in a parking lot. When the pole is positioned properly, it is perpendicular to the pavement. How can you check that the pole is perpendicular using a tape measure?

**Solution**

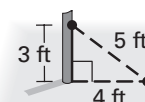
To show a line is perpendicular to a plane you must show that the line is perpendicular to two lines in the plane.

Think of the pole as a line and the pavement as a plane. Use a 3-4-5 right triangle and the Converse of the Pythagorean Theorem to show that the pole is perpendicular to different lines on the pavement.

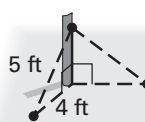
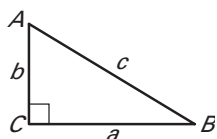
First mark 3 feet up the pole and mark on the pavement 4 feet from the pole.



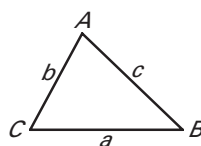
Use the tape measure to check that the distance between the two marks is 5 feet. The pole makes a right angle with the line on the pavement.



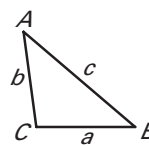
Finally, repeat the procedure to show that the pole is perpendicular to another line on the pavement.

**METHODS FOR CLASSIFYING A TRIANGLE BY ANGLES USING ITS SIDE LENGTHS****Theorem 7.2**

If  $c^2 = a^2 + b^2$ ,  
then  $m\angle C = 90^\circ$   
and  $\triangle ABC$  is a  
right triangle.

**Theorem 7.3**

If  $c^2 < a^2 + b^2$ ,  
then  $m\angle C < 90^\circ$   
and  $\triangle ABC$  is an  
acute triangle.

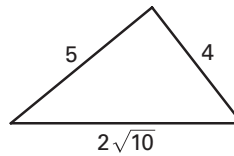
**Theorem 7.4**

If  $c^2 > a^2 + b^2$ ,  
then  $m\angle C > 90^\circ$   
and  $\triangle ABC$  is  
an obtuse  
triangle.

## Your Notes

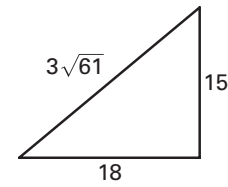
✓ **Checkpoint** In Exercises 1 and 2, tell whether the triangle is a right triangle.

1.



not a right triangle

2.



right triangle

3. Can segments with lengths of 6.1 inches, 9.4 inches, and 11.3 inches form a triangle? If so, would the triangle be *acute*, *right*, or *obtuse*?

Yes; obtuse

4. In Example 3, could you use triangles with side lengths 50 inches, 120 inches, and 130 inches to verify that you have perpendicular lines? *Explain*.

Yes; A triangle with side lengths 50 inches, 120 inches, and 130 inches is a right triangle. The right triangle shows that you have perpendicular lines.

## Homework