

1.6

Classify Polygons

Goal • Classify polygons.

Your Notes

VOCABULARY

Polygon

Sides

Vertex

Convex

Concave

n-gon

Equilateral

Equiangular

Regular

Your Notes

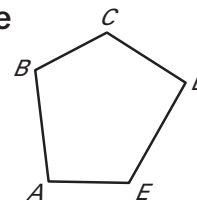
IDENTIFYING POLYGONS

In geometry, a figure that lies in a plane is called a *plane figure*. A _____ is a closed plane figure with the following properties.

1. It is formed by three or more line segments called _____.
2. Each side intersects exactly _____ sides, one at each endpoint, so that no two sides with a common endpoint are _____.

Each endpoint of a side is a _____ of the polygon. The plural of vertex is *vertices*.

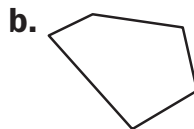
A polygon can be named by listing the vertices in consecutive order. For example, *ABCDE* and *CDEAB* are both correct names for the polygon at the right.



A *plane figure* is two-dimensional. Later, you will study three-dimensional *space figures* such as prisms and cylinders.

Example 1 Identify polygons

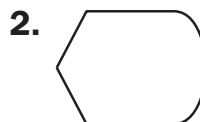
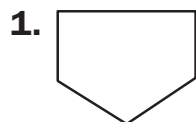
Tell whether the figure is a polygon and whether it is *convex* or *concave*.



Solution

- Some segments intersect more than two segments, so it is _____.
- The figure is _____.
- The figure is _____.

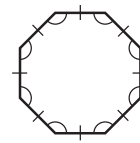
✓ **Checkpoint** Tell whether the figure is a polygon and whether it is *convex* or *concave*.



Your Notes

Example 2 Classify polygons

Classify the polygon by the number of sides. Tell whether the polygon is *equilateral*, *equiangular*, or *regular*.

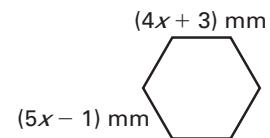


Solution

The polygon has 12 sides. It is equilateral and equiangular, so it is a regular dodecagon.

Example 3 Find side lengths

The head of a bolt is shaped like a regular hexagon. The expressions shown represent side lengths of the hexagonal bolt. Find the length of a side.



Hexagonal means "shaped like a hexagon."

Solution

First, write and solve an equation to find the value of x . Use the fact that the sides of a regular hexagon are congruent.

$4x + 3 = 5x - 1$ Write an equation.

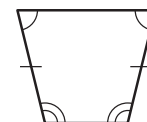
$-4x + 3 = 5x - 1$ Simplify.

Then evaluate one of the expressions to find a side length when $x = \underline{4}$. $4x + 3 = 4(\underline{4}) + 3 = \underline{19}$

The length of a side is 19 millimeters.

✓ Checkpoint Complete the following exercises.

3. Classify the polygon by the number of sides. Tell whether the polygon is *equilateral*, *equiangular*, or *regular*.



4. The expressions $(4x + 8)^\circ$ and $(5x - 5)^\circ$ represent the measures of two of the congruent angles in Example 3. Find the measure of an angle.

Homework